

**Applications Problems Involving Continuous Compounding**

There is a special growth formula that we use for problems involving continuous compounding.

**Continuous Compound Interest Formula**

$$y = a(e)^{r \cdot t}$$

$y$  = final amount       $a$  = starting amount       $r$  = rate (in decimal form)       $t$  = time

1. The growth of a bacteria colony in a petri dish can be modeled by the equation  $y = 75e^{-4t}$ , where  $t$  is the time in hours. Approximate the number of bacteria after two full days.  $t = 48$

$$y = 75e^{-4 \times 48} = \boxed{1.635 \times 10^{10}}$$

$$\begin{array}{r} 2020 \\ - 2004 \\ \hline 16 \end{array}$$

2. Your grandparents deposited \$500 into a trust fund for you the year you were born. If the bank paid 6.2% interest compounded continuously, what is the account balance today?

$$100 = .062$$

$$y = 500e^{.062 \times 16} = \boxed{1348.31}$$

$$y = 500e^{.062 \times 15} = \boxed{1267.25}$$

a?

3. Nalani plans to buy a new car in 5 years. How much should you deposit into a bank paying 7% continuous interest if she plans on spending \$20,000 for her car?

Compounded

$$20000 = a(e)^{.07 \times 5}$$

$$= \frac{20000}{e^{.07 \times 5}} = \boxed{14,093.76}$$

divide

$$r = .07$$

4. Nick is depositing money into an account paying 5.75% interest compounded continuously. How long will it take for his money to double?

$$t = ?$$

$$\frac{\$200}{\$100}$$

$$\frac{5.75\%}{100} = .0575$$

$$\frac{200}{100} = \frac{100}{100} e^{.0575 \times t}$$

$$\boxed{2} = e^{.0575 \times t}$$

$$\boxed{t = 12}$$